

Welbeck Primary School



Mathematics KS2 Calculation Policy

Reviewed September 2021



KEY STAGE 2 WRITTEN CALCULATION METHODS

Addition and Subtraction Objectives

<u>Year 3</u>	<u>Year 4 Objectives</u>	<u>Year 5 Objectives</u>	<u>Year 6 Objectives</u>
<ul style="list-style-type: none"> add and subtract numbers mentally, including: <ul style="list-style-type: none"> a three-digit number and ones a three-digit number and tens a three-digit number and hundreds add and subtract numbers with up to 3- digits using formal written methods of columnar + - estimate the answer to a calculation and use inverse operations to check answers solve problems ... more complex + - 	<ul style="list-style-type: none"> add and subtract numbers with up to 4-digits using the formal written methods of columnar + - estimate and use inverse operations to check answers to a calculation solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why. 	<ul style="list-style-type: none"> add and subtract whole numbers with more than 4 digits, including using formal written methods (column + -) add and subtract numbers mentally with increasingly large numbers use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy solve + - multi-step problems in contexts, deciding which operations and methods to use and why. 	<ul style="list-style-type: none"> use their knowledge of the order of operations to carry out calculations involving the four operations solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why

Addition Progression: builds upon secured KS1 written calculation methods

Column addition (Y2/Y3)

Column Addition (Y3 onwards)

$$\begin{array}{r} 789 \\ + 642 \\ \hline 1431 \\ \hline \end{array}$$

$\nearrow \nearrow$

Column Addition with decimals (Y5/Y6)

$$124.9 + 117.25 = 242.15$$

$$\begin{array}{r} 124.90 \\ + 117.25 \\ \hline 242.15 \\ \hline \end{array}$$

$\nearrow \nearrow$

Subtraction Progression: builds upon secured KS1 written calculation methods

Column subtraction (Y2/Y3)

$32 - 11 =$ $83 - 46 =$

Column subtraction (Y3 onwards)

$932 - 457$ becomes

$$\begin{array}{r} 8 \quad 12 \quad 1 \\ 932 \\ - 457 \\ \hline 475 \\ \hline \end{array}$$

Column subtraction with decimals (Y5/Y6)

$$\begin{array}{r} 1 \quad 1 \quad 4 \\ 22.50 \\ - 19.28 \\ \hline 03.22 \\ \hline \end{array}$$



KEY STAGE 2

WRITTEN CALCULATION METHODS

Multiplication and Division Objectives

<u>Year 3</u>	<u>Year 4 Objectives</u>	<u>Year 5 Objectives</u>	<u>Year 6 Objectives</u>
<ul style="list-style-type: none"> recall and use multipl/div facts for 3, 4 and 8 x tables write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects. 	<ul style="list-style-type: none"> recall mult/div facts for all x tables up to 12×12 use place value, known and derived facts to multiply and divide mentally, including multiplying by 0 and 1; dividing by 1; multiplying together three numbers recognise and use factor pairs and commutativity in mental cal multiply 2-digit/3-digit numbers by a 1-digit number using formal written layout solve problems involving $x +$, including the distributive law multiply 2-digit x 1-digit, integer scaling problems and correspondence problems such as n objects are connected to m objects. 	<ul style="list-style-type: none"> identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers Know, use the vocab of prime numbers, prime factors and composite (non- prime) no's understand if a number up to 100 is prime and recall prime numbers up to 19 x numbers up to 4 digits by a 1/2-digit number using a formal written method, including long multiplication for 2-digit nos mult/divide numbers mentally drawing upon known facts divide numbers up to 4 digits by a 1-digit number using the formal written method of short div and interpret remainders $x \div$ whole numbers and nos involving decimals by 10/100/ 1000 	<ul style="list-style-type: none"> x multi-digit numbers up to 4 digits by a 2-digit whole number using formal written long x divide numbers up to 4 digits by a 2-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, in context divide numbers up to 4 digits by a 2-digit number using the formal written method of short division where appropriate, interpreting remainders in context mental calculations with mixed operations and large numbers identify common factors, multiples and prime nos use knowledge of the order of operations to carry out calculations involving 4 operations BODMAS

Multiplication Progression: builds upon secured KS1 written calculation methods

Multiplication (Y2/Y3)

Partitioning using the grid method

$$\begin{array}{r|l} 32 \times 3 = 96 \\ \hline \begin{array}{r} x \\ 3 \end{array} & \begin{array}{r} 30 \\ 90 \end{array} & \begin{array}{r} 2 \\ 6 \end{array} \end{array}$$



Short multiplication

$$\begin{array}{r} 237 \\ \times 4 \\ \hline 948 \end{array}$$

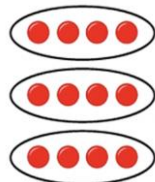


Long Multiplication

$$\begin{array}{r} 458 \\ \times 42 \\ \hline 916 \\ 18320 \\ \hline 19236 \end{array}$$

Division Progression: builds upon secured KS1 written calculation methods

Division as sharing (Y2/Y3)



$$12 \div 4 = 3$$



Bus stop division

$$98 \div 7 =$$

$$\begin{array}{r} 14 \\ 7 \overline{) 98} \end{array}$$

$$98 \div 7 =$$

$$\begin{array}{r} 086 \text{ r}2 \\ 5 \overline{) 432} \end{array}$$



Division

$$\begin{array}{r} 42 \\ 19 \overline{) 798} \end{array}$$

$$\begin{array}{l} 1 \times = 19 \\ 2 \times = 38 \\ 3 \times = 57 \\ 4 \times = 76 \\ 5 \times = 95 \\ 6 \times = 114 \\ 7 \times = 133 \\ 8 \times = 152 \\ 9 \times = 171 \\ 10 \times = 190 \end{array}$$

KEY STAGE 2

WRITTEN CALCULATION METHODS: FRACTIONS



Addition/Subtraction

$$\frac{1}{5} + \frac{3}{4} =$$

Strategy: identify the LCM (lowest common multiple). LCM of 5 and 4 is 20. Convert.

$$\frac{1}{5} \xrightarrow{\times 4} \frac{4}{20} \quad \frac{3}{4} \xrightarrow{\times 5} \frac{15}{20}$$

$$\frac{4}{20} + \frac{15}{20} = \frac{19}{20}$$

Answer: $\frac{19}{20}$

$$1\frac{1}{5} + 2\frac{1}{10} =$$

Strategy: convert both mixed numbers into improper fractions

$$1\frac{1}{5} + 2\frac{1}{10} = \frac{6}{5} + \frac{21}{10}$$

Next step: identify the LCM (lowest common multiple). LCM of 5 and 10 is 10. Convert.

$$\frac{6}{5} \xrightarrow{\times 2} \frac{12}{10} \quad \frac{21}{10} \xrightarrow{\times 2} \frac{42}{20}$$

Next step: add the two improper fractions

$$\frac{12}{10} + \frac{21}{10} = \frac{33}{10}$$

Answer: $3\frac{3}{10}$ given as a mixed number

Multiplication/Division

$$\frac{2}{3} \div 3 =$$

Strategy: convert the whole number into a fraction ('Top' it)

$$\frac{2}{3} \div \frac{3}{1}$$

Next step: invert the divisor ('Flip' it)

$$\frac{2}{3} \div \frac{1}{3}$$

Next step: change \div to \times

$$\frac{2}{3} \times \frac{1}{3} = \frac{2}{9}$$

Answer: $\frac{2}{9}$

$$2\frac{2}{5} \times 3 =$$

Strategy: convert the mixed number into an improper fraction and the whole number 3 into a fraction

$$2\frac{2}{5} = \frac{12}{5} \quad 3 = \frac{3}{1}$$

Next step: multiply

$$\frac{12}{5} \times \frac{3}{1} = \frac{36}{5}$$

Answer: $7\frac{1}{5}$ given as a mixed number

Dividing fraction by whole number

$$\frac{2}{3} \div 3$$

Convert each denominator into the LCM = 3

$$\frac{2}{3} \div \frac{3}{1} \xrightarrow{\times 3} \frac{9}{3}$$

$$\frac{2}{3} \div \frac{9}{3} = \frac{2}{9} = \frac{2}{9}$$



KEY STAGE 2

WRITTEN CALCULATION METHODS: FRACTIONS

Fraction of an amount

Fraction of an amount

2/3 of 3693 =

Strategy: divide the whole number by the denominator ('bottom') to calculate 1/3. Use the bus-stop method.

$$\begin{array}{r} 1231 \\ 3 \overline{) 3693} \end{array}$$

Next step: then multiply this new number by the numerator ('top') to calculate 2/3

$$\begin{array}{r} 1231 \\ \times \quad 2 \\ \hline 2462 \end{array}$$

Answer: 2462

$$\frac{5}{6} \times 540 =$$

Strategy: divide the whole number by the denominator ('bottom') to calculate 1/6. Use fluency: if $54 \div 6 = 9$, then

$$540 \div 6 = 90$$

Next step: then multiply this new number by the numerator ('top') to calculate 5/6

$$90 \times 5 = 450$$

Fluency links: $9 \times 5 = 45$, so $90 \times 5 = 450$

Fractions of an amount

Fraction of an amount

1/4 of 1000 =

Strategy: recognise that to find a $\frac{1}{4} = \frac{1}{2}$ and $\frac{1}{2}$ again

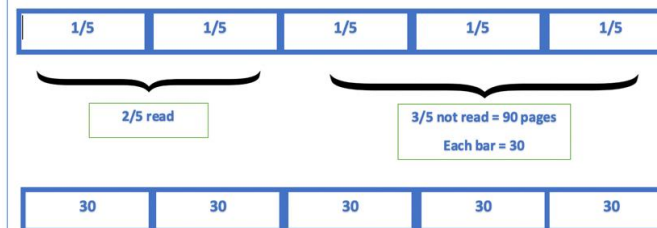
$\frac{1}{2}$ of 1000 = 500, $\frac{1}{2}$ of 500 is 250.

Fluency links: $\frac{1}{2}$ of 50 = 25, so $\frac{1}{2}$ of $500 = 250$

Fractions of an amount – Bar Model Method

Fractions of an amount/Bar Model

On Saturday Lara read $\frac{2}{5}$ of her book.  On Sunday she read the **other** 90 pages to finish the book. How many pages are there in Lara's book?



Total pages = $30 + 30 + 30 + 30 + 30 = 150$



KEY STAGE 2

WRITTEN CALCULATION METHODS: DECIMALS

Multiplying/Dividing decimals

Multiplying/Dividing decimals

$$3.9 \times 30 =$$

Strategy: use column multiplication.

$$\begin{array}{r} 30 \\ \times 3.9 \\ \hline 270 \\ + 900 \\ \hline 1170 \end{array}$$

3.9 has one decimal place so answer will have one decimal place.

Multiplying/Dividing decimals

$$15 \times 6.1 =$$

Strategy: use column multiplication.

$$\begin{array}{r} 15 \\ \times 6.1 \\ \hline 15 \\ + 90 \\ \hline 915 \end{array}$$

6.1 has one decimal place so answer will have one decimal place.

Multiplying/Dividing decimals

$$73.8 \div 6 =$$

Strategy: use bus stop division method.

$$\begin{array}{r} 12.3 \\ 6 \overline{) 73.8} \end{array}$$

Answer: 12.3

Multiplying/Dividing decimals

$$70 \div \square = 3.5$$

Strategy: identify inverse method.

$$70 \div 3.5 = \square$$

Next step: multiply both numbers by 10 so that both are whole numbers

$$700 \div 35 = \begin{array}{r} 020 \\ 35 \overline{) 700} \end{array}$$

Answer: 20

Multiplying/Dividing by multiples of 10, 100, 1000

Multiples of 10/100/1000

$$0.9 \div 100 =$$

Strategy: underline and count the zeros (x2):

$$\underline{0.9} \div \underline{100} =$$

Next step: Add in place holders to 0.9.

$$\underline{0.009} \div 100 =$$

Next step: divide by 100 by moving the decimal point 2 places to the left

$$\begin{array}{c} \curvearrowright \curvearrowright \\ 00\underline{0.9} \div 100 = 0.009 \end{array}$$

Answer: 0.009

Multiples of 10/100/1000

$$5.014 \times 10 =$$

Strategy: underline and count the zeros (x1):

$$\underline{5.014} \times \underline{10} =$$

Next step: move the decimal place **one** place to the right using arrows

$$\begin{array}{c} \curvearrowright \\ \underline{5.014} \times 10 = 50.14 \end{array}$$

Answer: 50.14

Multiples of 10/100/1000

$$34.8 \times 1,000 =$$

Strategy: underline and count the zeros (x3):

$$\underline{34.8} \times \underline{1000} =$$

Next step: Add in place holders

$$\underline{34.800}$$

Next step: move the decimal point **three** places to the right using arrows

$$\begin{array}{c} \curvearrowright \curvearrowright \curvearrowright \\ 34\underline{800} \times 1000 = 34800 \end{array}$$

Answer: 34800

Multiples of 10/100/1000

$$0.9 \times 200$$

Strategy: partition 200 into 100 and 100

$$0.9 \times 100$$

$$0.9 \times 100$$

Next step: move decimal point 2 decimal places to the right. Use placeholders

$$\begin{array}{c} \curvearrowright \curvearrowright \\ 0.9 \times 100 = 09\underline{00} \end{array}$$

$$0.9 \times 100 = 90$$

Answer: 90 + 90 = 180

Multiples of 10/100/1000

$$343.1 \div 1000 =$$

Strategy: underline and count the zeros (x3):

$$343.1 \div \underline{1000} =$$

Using arrows, move the decimal point **3** places to the left:

$$\begin{array}{c} \curvearrowright \curvearrowright \curvearrowright \\ 343\underline{.1} \div 1000 = 0.343 \end{array}$$

Answer: 0.343



KEY STAGE 2

WRITTEN CALCULATION METHODS: PERCENTAGES

25% of 88 = 22

Strategy: recognise that 25% is the same as $\frac{1}{4}$

To find a $\frac{1}{4}$ = $\frac{1}{2}$ and $\frac{1}{2}$ again

$\frac{1}{2}$ of 88 = 44, $\frac{1}{2}$ of 44 = 22

Answer: 22

20% of 3,000 =

Strategy: use understanding of calculating 10% and that 20% is two lots of 10% (doubling)

10% of 3000 = 300

20% of 3000 = 300 x 2 = 600

Answer: 600

28% x 650 =

Strategy: partition 28% into 10%, 10% and 8%.

10% of 650 = 650 \div 10 = 65

10% of 650 = 650 \div 10 = 65

8%: 1% of 650 = 650 \div 100 = 6.5

8% = 6.5 x 8 = 52

Answer: 65 + 65 + 52 = 182

45% of 460 =

Strategy: use understanding that 45% can be partitioned into 4 lots of 10%, and 5%.

10% of 460 = 460 \div 10 = 46

40% = 46 x 4 = 184

5% = $\frac{1}{2}$ of 10% = $\frac{1}{2}$ of 46 = 23

Answer: 184 + 23 = 207

51% of 900 =

Strategy: recognise that 50% is the same as $\frac{1}{2}$

Use understanding of fluency that $\frac{1}{2}$ of 90 = 45, so $\frac{1}{2}$ of 900 = 450

$\frac{1}{2}$ of 900 = 450

1% = 900 \div 100 = 9

Answer: 450 + 9 = 459

17% x £26 =

*Strategy: partition 17% into 10% and 7%.
Decimalise £26 to £26.00*

10% of £26 = 26.00 \div 10 = 2.6

7%: 1% of £26.00 = 26.00 \div 100 = 0.26

7% = 0.26 x 7 = 1.82

Answer: 2.6 + 1.82 = 4.42

KEY STAGE 2

WRITTEN CALCULATION METHODS: MISCELLANEOUS

Factors

A **factor** is a number that divides into another number exactly and without leaving a remainder.

Factors:

1, 2, 3, 4, 6, 12

$12 \div 1 = 12$	<p>Stop when repeats.</p>
$12 \div 2 = 6$	
$12 \div 3 = 4$	
$12 \div 4 = 3$	
$12 \div 5 =$	

EAL scaffolding

Words <ul style="list-style-type: none"> Add More than Plus Total/ total value Increase The sum of... Altogether How many? How many altogether 	Number sentence <p>• $3 + 8 = 11$</p> <p>• $4 + 5 = 9$</p> <table border="1" style="font-size: small; margin-top: 5px;"> <tr><td>2</td><td>3</td></tr> <tr><td>+</td><td>4 2</td></tr> <tr><td colspan="2">6 5</td></tr> </table> <table border="1" style="font-size: small; margin-top: 5px;"> <tr><td>3</td><td>2</td><td>4</td></tr> <tr><td>+</td><td>2</td><td>5 6</td></tr> <tr><td colspan="3">5 8 0</td></tr> <tr><td colspan="3">1</td></tr> </table>	2	3	+	4 2	6 5		3	2	4	+	2	5 6	5 8 0			1			<div style="background-color: #0056b3; color: white; padding: 10px; font-weight: bold; font-size: 1.2em;">Addition</div>
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+	4 2																			
6 5																				
3	2	4																		
+	2	5 6																		
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1																				
Images			<p>Have a go!</p>																	

Words <ul style="list-style-type: none"> Take away Subtract Minus Take off Less than Decrease What is the difference? How many/much are/is left over? How many more... How much change... 	Number sentence <p>• $7 - 3 = 4$</p> <p>• $16 - 8 = 8$</p> <p>• $32 - 2 = 30$</p> <table border="1" style="font-size: small; margin-top: 5px;"> <tr><td>4</td><td>9</td><td>8</td><td>12</td></tr> <tr><td>-</td><td>3</td><td>7</td><td>5</td></tr> <tr><td colspan="4">1 1 7</td></tr> </table> <table border="1" style="font-size: small; margin-top: 5px;"> <tr><td>4</td><td>9</td></tr> <tr><td>-</td><td>2 7</td></tr> <tr><td colspan="2">2 2</td></tr> </table>	4	9	8	12	-	3	7	5	1 1 7				4	9	-	2 7	2 2		<div style="background-color: #e67e22; color: white; padding: 10px; font-weight: bold; font-size: 1.2em;">Subtraction</div>
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1 1 7																				
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Images			<p>Have a go!</p>																	

Words <ul style="list-style-type: none"> Share Equal groups of Divide Equal Split up 	Number sentence <p>• $15 \div 3 = 5$</p> <p>• $8 \div 2 = 4$</p> <p>• $9 \div 3 = 3$</p>	<div style="background-color: #2e7d32; color: white; padding: 10px; font-weight: bold; font-size: 1.2em;">Division</div>	
Images			<p>Have a go!</p>

Words <ul style="list-style-type: none"> Lots of Groups of Array Multiply Times Repeated addition How many times larger... 	Number sentence <p>• $2 \times 6 = 12$</p> <p>• $4 \times 5 = 20$</p> <table border="1" style="font-size: small; margin-top: 5px;"> <tr><td>1</td><td>4</td></tr> <tr><td>X</td><td>3</td></tr> <tr><td colspan="2">4 2</td></tr> </table> <table border="1" style="font-size: small; margin-top: 5px;"> <tr><td>2</td><td>3</td></tr> <tr><td>X</td><td>4 2</td></tr> <tr><td colspan="2">4 6</td></tr> <tr><td colspan="2">9 6 6</td></tr> </table>	1	4	X	3	4 2		2	3	X	4 2	4 6		9 6 6		<div style="background-color: #673ab7; color: white; padding: 10px; font-weight: bold; font-size: 1.2em;">Multiplication</div>
1	4															
X	3															
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Images			<p>Have a go!</p>													